

# AlZnO magnetron sputtered thin film for photovoltaic application

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**Abstract:** Aluminum zinc oxide (AZO) is a nontoxic and a low-cost material that finds application as a transparent conducting electrode in photovoltaic devices. In this study the (direct current) DC magnetron sputtering of AZO films is carried out at different deposition times of 5, 10, 15, 20 and 25 min's at room temperature and it's structural, optical, electrical and morphological properties are studied for its use as a front contact for thin film solar cell application. The structural study suggests that the preferred orientation of grains along (002) plane having hexagonal structure and the optical and the electrical studies suggest that the films show an average transmission of 70% and a resistivity of the order of  $10^{-4}\Omega\text{cm}$ . On the other hand, the scanning electron microscopy (SEM) images suggest the formation of packed grains having a homogeneous surface. Moreover in order to study the optoelectronic properties of prepared samples, the electronic and optical calculations of the AZO are performed by the first-principles calculations using density functional theory (DFT).

**Keywords:** AZO; sputtering; photovoltaic; thin film solar cell; DFT

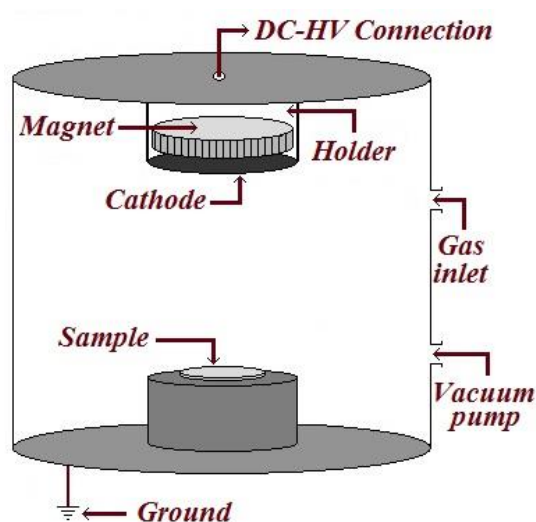
## 1. Introduction

Aluminum zinc oxide (AZO) is a transparent conducting oxide (TCO) material owing to its nontoxicity as well as its tunable optoelectronic properties [1–5]. AZO thin films are widely used in photonic devices such as light-emitting diodes (LED's) [6], thin film solar cells [7,8], flat panel displays [9] as well as sensing devices [10,11]. It is notable that the above applications requires conductivity of (sheet resistance  $<10$  ohms per square) as well as high transmittance ( $>80\%$ ) in the visible region. There are different techniques to prepare AZO films such as sputtering [12], electron beam evaporation, [13], pulsed laser deposition [14], chemical vapor deposition [15], spray pyrolysis [16], and sol–gel deposition [17] that are well reported for preparing AZO thin films on different substrates. Direct current (DC) magnetron sputtering is an industrially acceptable technique due to its convenience in high deposition rate and scalability on a large area [18]. Generally speaking, most commonly preferred substrate of all TCO films is glass and physical properties of sputtered AZO thin films are highly sensitized on controlled process parameters such as base vacuum, gas pressure, substrate temperature and deposition time. Therefore in this study optimized experimental conditions are found to investigate the effect of deposition time on the physical properties of AZO thin film deposited on soda lime glass substrate. The effect of deposition time is estimated on the structural, optical, morphological, and electrical properties, in order to achieve the lowest resistivity and the highest transparency for

the films. On the other hand, the electronic and optical calculations of the AZO films are also performed by the first-principles calculations using DFT in order to achieve more detail studies on the prepared AZO thin film.

## 2. Materials and methods

**Figure 1** shows schematic diagram of a magnetron sputtering system, which is used in this experiments. AZO thin films are deposited using magnetron sputtering setup from a 3 inch diameter target consisting of 98 wt % ZnO and 2 wt % Al<sub>2</sub>O<sub>3</sub>. It is worth nothing that the films are deposited at room temperature and no oxygen is introduced in this process. First of all, the glass substrates are ultrasonically cleaned in sequentially distilled water, acetone, alcohol, distilled water and finally are dried with nitrogen gas. The substrates are then placed at 70 mm distance from the target. The sputtering chamber is firstly pumped to a base vacuum pressure of  $10^{-6}$  Torr and the Ar gas is introduced into the chamber. The sputtering gas pressure is set to be about  $2 \times 10^{-2}$  Torr. After the deposition, the samples are self cooled and later are examined for their physical properties. The surface morphology of the films and the crystal structure are studied using a field effect scanning electron microscope (FESEM) and the X-ray diffractometer (XRD), respectively. A Dektak Profilometer is also used to estimate the films thicknesses. The optical transmission measurements are also carried out with a spectrophotometer in the spectral region of 190–800 nm and the atomic force microscope (AFM) images are also taken under the contact mode to evaluate the roughness of the films. Moreover, the resistivities of the films are measured using a four-point probe method.



**Figure 1.** Schematic of magnetron sputtering setup.

## 3. Results

### 3.1. Experimental

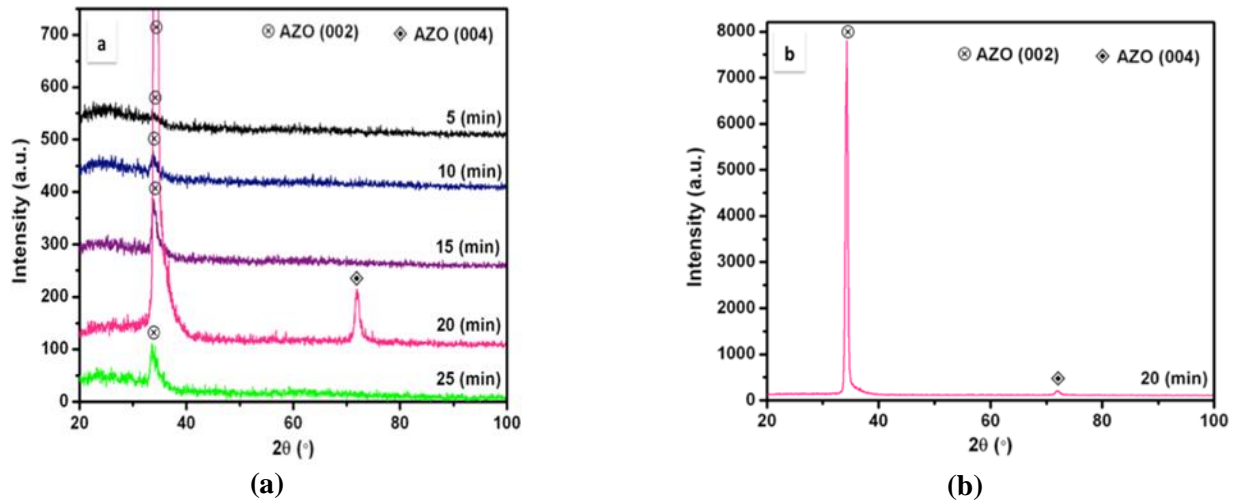
AZO thin films prepared at different deposition times while keeping other experimental conditions constant are studied for their physical properties. By increasing the deposition time the film thicknesses are increased as well. **Table 1** gives

the thicknesses of the AZO thin films prepared at different deposition times of 5, 10, 15, 20 and 25 min.

**Table 1.** Thicknesses of the AZO thin films prepared at different deposition times.

Thickness	Deposition Time
210 nm	5 min
350 nm	10 min
520 nm	15 min
710 nm	20 min
1150 nm	25 min

**Figure 2a** shows the XRD spectra of AZO films grown at different deposition times. From XRD data's 5 min is not enough time to form the film and the XRD data does not show any AZO peak. However, The Film grown at the deposition time of 20 min shows a (002) peak with high intensity, which becomes much stronger, sharper and narrower. A small diffraction intensity from (004) planes are also appears in the XRD spectra. As it can be seen from a **Figure 2b** the (004) peak intensity is very low in comparison with (002) peak intensity. Both peaks belong to AZO structures with two different planes. Moreover, a higher XRD intensity corresponds to improved film crystallinity for 20 min. It is clear that all the the polycrystalline AZO thin films deposited on the glass substrates exhibit (002) crystallographic orientation due to the minimal surface energy in the ZnO hexagonal wurtzite structure. Appearance of (002) peak in this spectra, indicating that the films grown at different deposition times have a c-axis preferred orientation due to a self texturing phenomenon [16].



**Figure 2.** XRD spectra of AZO films deposited at (a) various deposition times; (b) 20 min.

From the XRD spectrum the crystalline quality of the AZO thin films become weak for the higher deposition times (25 min) and no peaks corresponding to Al<sub>2</sub>O<sub>3</sub> phase are seen in the XRD pattern, which maybe due to the aluminum replacing zinc, substitutionally in the hexagonal lattice. From the XRD data, the average grain size of AZO thin film can be also evaluated by Debye-Scherrer equation [16] as follows:

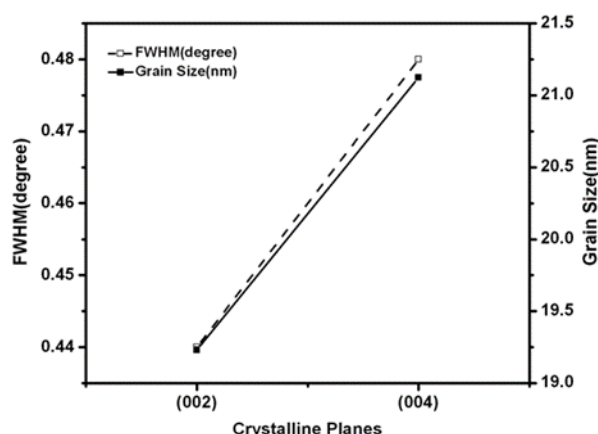
$$\text{Grain size} = 0.9 \lambda / \beta \cos \theta \quad (1)$$

where  $\lambda$  is the X-ray wavelength (0.154 nm),  $\theta$  is the Bragg angle, and  $\beta$  is the full width at half maximum (FWHM) of the diffraction peak. The calculated crystal sizes of the thin films are more or less uniform for all the films, ranging from 8 to 19 nm (**Table 2**). The maximum grain size is around 19.231 nm for the sample prepared at the 20 min deposition time.

**Table 2.** Calculated grain sizes and FWHM for AZO films grown at different deposition times for (002) peaks.

Time (min)	D-Spacing (Å)	FWHM (degree)	Grain Size (nm)
5	2.659	0.59	14.483
10	2.656	0.96	8.725
15	2.654	0.72	11.680
20	2.618	0.44	19.231
25	2.673	0.6	14.053

**Figure 3** shows the graph of the FWHM of (002) and (004) XRD peaks and the corresponding grain sizes of the AZO thin films as a function of crystal planes. It is observable that the grain size for the (004) peak is larger and the average grain size for the both AZO crystal planes is around 20 nm.

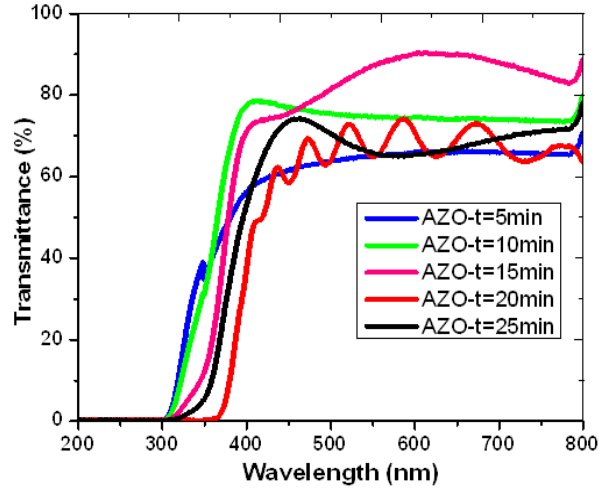


**Figure 3.** FWHM and grain size of (002) and (004) XRD peaks corresponding to the AZO thin film as a function of crystal planes.

**Figure 4** shows the optical transmittance of the AZO thin films measured by UV-VIS spectrophotometer in the frequency range of the 200–800 nm. All the thin films sputtered at the different deposition times exhibit more than 70% transmittance in the visible region.

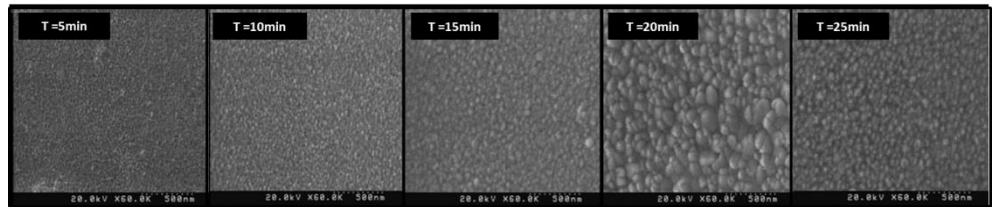
An excellent surface quality and a homogeneity of the film are confirmed from the appearance of the interference fringes in the transmission spectra occurring when the film surface is reflecting without much scattering/absorption in the bulk of the film [17]. As it can be seen in the **Figure 5** the film which, is prepared at 20 min shows these interference fringes. Electrical resistivity of the films are also given in **Table 3** for the different deposition times prepared samples. The lowest resistivity of the films is measured to be  $4.1 \times 10^{-4}$ . It can be seen that the resistivity increases as the deposition time increases to 20 min and then decreases as the deposition time increases

at 25 min. Increasing the crystallite size of AZO thin films can decrease the grain boundary scattering and increase the carrier lifetime to achieve the lower resistivity of the AZO thin films.



**Figure 4.** The transmission over the VIS range for AZO thin film at different deposition times.

SEM images of AZO are shown in a **Figure 5**. These images can be used to study the AZO film surface morphology and microstructure, which show the surface micrographs of the films as a function of the deposition time. It is found that the deposition time has a great influence on the film surface structure. The AZO film deposited at 20 min shows surface features of densely packed grains and the grains that are aggregating.



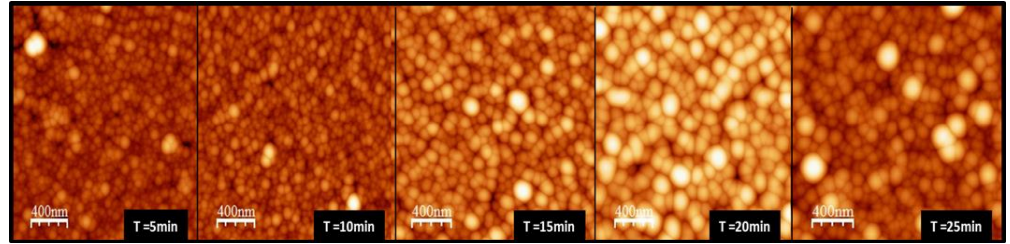
**Figure 5.** SEM images of AZO thin films at different deposition times.

**Table 3.** Electrical resistivities measured for the AZO thin films prepared at different deposition times.

Resistivity ( $\Omega\text{cm}$ )	Deposition time
$9.8 \times 10^{-2}$	5 min
$3.6 \times 10^{-2}$	10 min
$3.2 \times 10^{-3}$	15 min
$4.1 \times 10^{-4}$	20 min
$1.2 \times 10^{-3}$	25 min

Moreover, AFM images are given in **Figure 6** for the AZO thin films deposited at different deposition times. It is known that the surface roughness is one of the important factors of the AZO thin film for many optoelectronic applications, because

the level of surface roughness will dominate the carrier mobility and the light scattering [19,20]. In the **Figure 6** rough and non-uniform surface structures of the AZO thin films at the different deposition times are observed. The roughnesses of the films are given in the **Table 4**. As it can be seen the roughness is increased by increasing the deposition time to 20 min due to the density of the thin film, which is enhanced by increasing the deposition time.



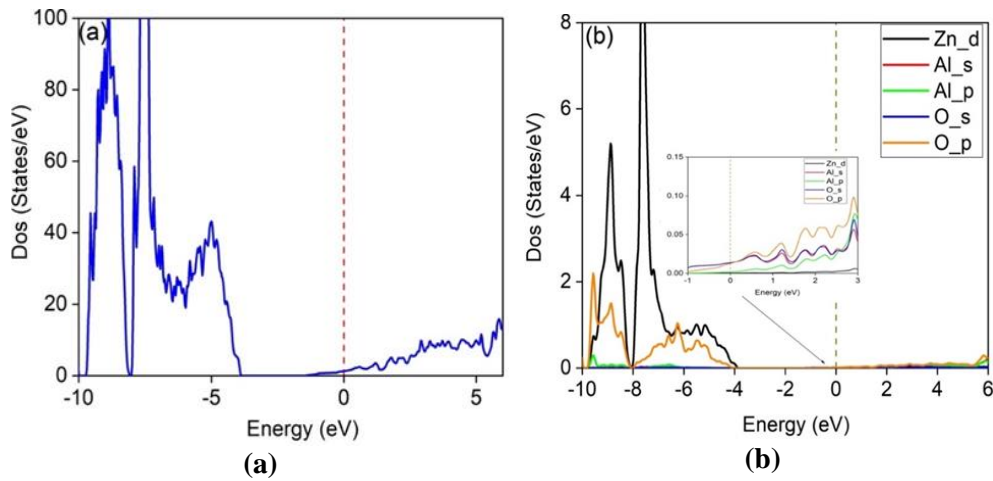
**Figure 6.** AFM images of AZO thin films deposited at different deposition times.

**Table 4.** Average roughnesses of the AZO thin films deposited at different deposition times.

Roughness	Deposition Time
28.4 nm	5 min
33.4 nm	10 min
48.7 nm	15 min
49.3 nm	20 min
38.4 nm	25 min

### 3.2. Computational

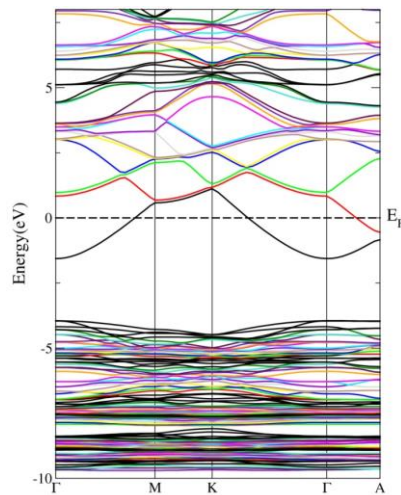
The electronic, and optical calculations of the AZO film are performed by the first-principles calculations using density functional theory (DFT) [21–23]. Solving the Kohn-Sham equations are done using the full potential method of linear augmented waves (FP-LAPW) [24], which is used in the WIEN2k package [25]. PBE-GGA approximation is used to solve the Exchange-Correlation potential for more accuracy [26]. The optimized input parameters including RKmax, KPoint, lmax and separation energy are selected as 8.0,  $10 \times 10 \times 2$ , 10 and  $-7.0$  Ryd, respectively. The muffin tin values of the Zn, O, and Al atoms are selected to 2.20 a.u., 1.45 a.u. and 1.8 a.u., respectively. The forces convergence of the relaxation calculations are  $10^{-6}$  dyn/a.u. and the optical calculations are approximated by the random phase approximation (RPA) with  $15 \times 15 \times 2$  KPoint in the first Brillouinzone. In **Figure 7**, panel (a), the density of electronic states (DOS) of ZnO with Al impurity of 2% is calculated with mBJ approximation. This diagram shows that this compound has a very weak conductivity because the electron states are partially present in the Fermi level, and in the region below the Fermi level (valence area), a 2 eV gap is seen. In the  $-4$  eV region, there are many electron states towards the lower energies of the valence region, and also in the region of  $-4$  eV to  $-9.5$  eV the Van Hov singularity is observed. Therefore, during the radiation or applying the heat, there is a suitable source for excited electrons. In panel (b) the partial DOS are shown.



**Figure 7.** (a) the density of electronic states (DOS) of ZnO with Al impurity of 2%; (b) the partial DOS.

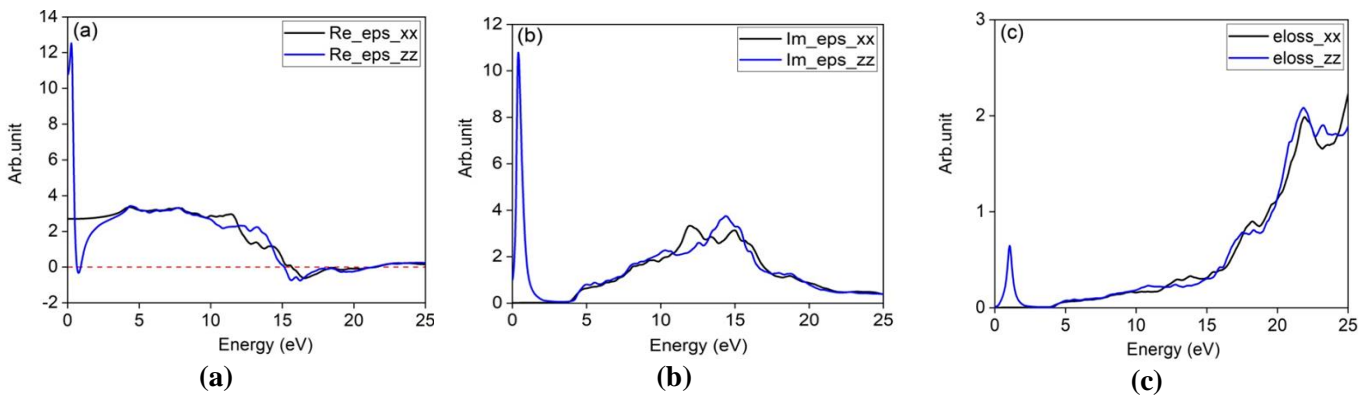
It can be seen that in the valence region, the main contribution of the density of electronic states belongs to the d-Zn and p-O orbitals, and the p-O, s-O, and s-Al orbitals have the main role at Fermi level and conduction region.

In **Figure 8**, the band structure of ZnO:Al with 2% impurity percentage is depicted in the symmetry direction  $M \rightarrow K \rightarrow \Gamma \rightarrow A \rightarrow \Gamma$  in the first Brillouin zone. It can be seen that in the region of  $-9.5$  eV to  $-4$  eV, a high density of electron levels are shown, which is in perfect agreement with the DOS curves. In the region of  $-4.5$  eV to  $-1.5$  eV and above  $-1.5$  eV of the Fermi level, an energy gap and electron level belonging to the s-Al orbital are given, respectively, which intersects the Fermi level. Due to the appropriate slope of this level curve, it helps the excited electrons to move to the conduction region. Another point is that the gradient of the conduction region is higher than the valence region, so the excited electrons are well placed in the conduction current.



**Figure 8.** the band structure of AZO with 2% impurity percentage in the first Brillouin zone.

In **Figure 9**, the optical diagrams of this compound are examined. Due to the inclusion of Al impurity in the ZnO structure, its cubic symmetry is disturbed. Due to the asymmetry in the arrangement of atoms after the Al impurity atom enters the ZnO compound, the response of this compound to the light irradiated in different directions is different. Therefore, the optical behavior of AlZnO compound was investigated in two crystal directions, x and z, which we have distinguished in the optical diagrams. Panel (a) shows the real part of the dielectric function, whose static value along the z-axis shows the poor metallic behavior. However, as soon as the energy of the radiated photon increases, the dielectric function diagram is strongly reduced in Dirac form and reduced to zero and negative values and it is reached to 2.7 in the UV and visible region. It remains constant up to the range of 8 eV.



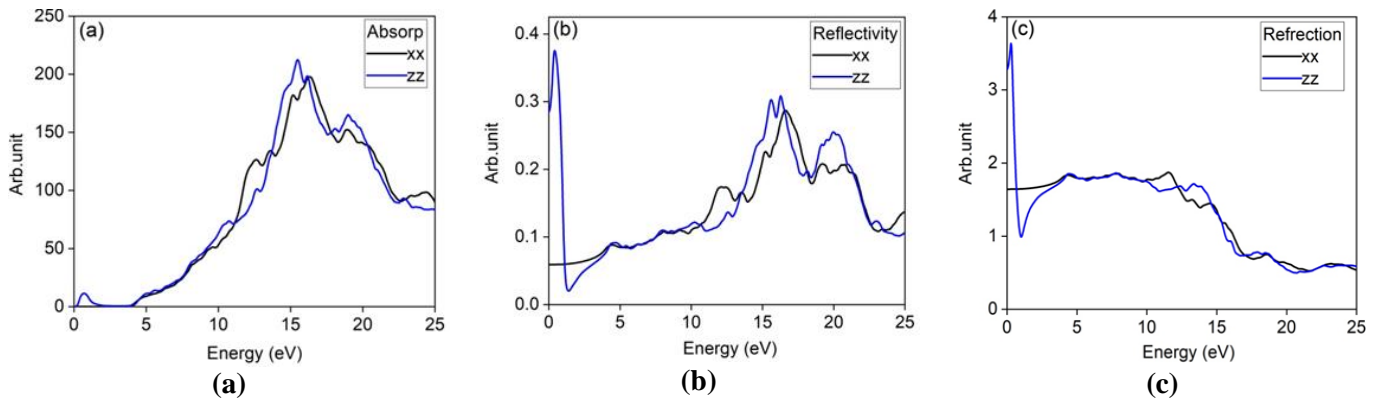
**Figure 9.** (a) real part; (b) imaginary part; (c) the spectrum of the loss of dielectric function in both x and z directions.

With radiation along the x-axis, its static value is 2.7 and it remains in this range up to 10 eV. From 10 eV onwards, this function is reduced in both directions, and at 15 eV to 20 eV, it will have negative values. The low value of the true dielectric function of this composition can be an indicator of the transparency of this composition. Panel (b) shows the imaginary part of the dielectric function in both x and z directions. Along the z-axis, we see a sharp Dirac peak that becomes zero with the increase of the emitted photon energy at the visible edge, which is consistent with the metallic behavior of this composition. Along the x-axis up to the range of 4 eV of the UV edge, a gap that increases with the increase in the energy of the irradiated photon is seen and it is reached its maximum values from 15 to 14 eV, therefore, the electron transition occurs more at high energy. In panel (c), the spectrum of the loss function can be seen. There is a small peak in the z direction in the infrared range, which confirms the behavior of the metal. In the visible and uv range, the loss values are very small and the most loss is occurred in the 15 eV region. By comparing this diagram with the previous two diagrams, the transparency of this optical behavior in the infrared, visible and UV regions is confirmed.

In **Figure 10**, absorption, reflection coefficient, refraction coefficient for the AZO composition are drawn. As can be seen in the absorption diagram, there is practically no absorption up to the UV edge, except for a very small peak in the direction of the z-axis, which, comparing to the curves in **Figure 7**, it is concluded that this compound acts like a transparent material in visible, UV and the ir regions,. Also, with the increase in the energy of the emitted photon, the amount of absorption



increases in both directions. In panel (b), the reflection coefficient is specified for these two directions. In the z direction, its static value is around 30%, which, of course, decreases sharply with the increase of the radiated energy and increases in the visible region. In the x direction, the value of the reflection coefficient at low energies is around 8% and with the increase in the energy of the radiated photon, even up to the range of 15 eV, the value of the reflection coefficient for both directions is in the range of 5% to 30%, and in the IR, visible and UV regions is below 10%, which again emphasizes the transparency of this composition. In panel (c), the refractive index can be seen that its static value is 3.2 along the z axis and 1.7 along the x axis. In the direction of the z axis, an anisotropy can be observed at low energies, which is indicative of the poor metallic behavior, but with the increase of the energy of the radiated photon in both directions, the refractive index is less than 2. To 10eV and more, indicates the behavior of vacuum. It is the kind that has confirmed the transparency of the composition again.



**Figure 10.** (a) absorption, (b) reflection coefficient, (c) refraction coefficient for AZO composition.

#### 4. Discussion

AZO films are magnetron sputtered on the glass substrate at room temperature using DC magnetron sputtering to find optimum experimental condition to make front contact for optoelectronic devices. The structural, morphological, optical and electrical properties are studied, which suggest that preferred orientation of grains along (002) plane having hexagonal structure are grown at 20 min deposition time, that show packed grains with homogeneous surface. Moreover, this sample show an average transmission of 70% and a resistivity of the order of  $10^{-4} \Omega\text{cm}$ . On the other hand, the electronic and optical calculations of the AZO are performed by the first-principles calculations using density functional theory (DFT) to study more details on the physical properties of the films. DFT calculations results also reveal that this compound acts like a transparent material. Therefore, experimental and theoretical results are in good agreements and confirm that the grown film have promising TCO material for optoelectronic applications.

#### 5. Conclusion

Structural, electrical, morphological and optical properties of AZO films deposited at room temperature on glass substrates by magnetron sputtering are

investigated to explore a possibility of producing transparent oxide films through simple low cost process for photovoltaic applications. It is observed that the AZO thin films are grown with c-axis preferred orientations without degradation of wurtzite ZnO structure. Electrical and optical properties of the AZO films improved with increasing the deposition time. The higher crystallinity, lower resistivity, suitable roughness and transmittance obtained for the sample prepared at 20 min deposition time. The electronic, and optical calculations of the AZO are also performed by the first-principles calculations using DFT for ZnO:Al composition with 2% impurity percentage. This work suggest a possibility of producing AZO films with required electrical and optical properties by simple low cost process at room temperature.

**Author contributions:** Experimental, ZG; software, AB, AY and NV; draft preparation; MJ and PG. All authors have read and agreed to the published version of the manuscript.

**Conflict of interest:** The authors declare no conflict of interest.

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