

Editorial

Transforming frontiers: The next decade of differential equations and control processes

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CITATION

He JH. Transforming frontiers: The next decade of differential equations and control processes. Advances in Differential Equations and Control Processes. 2025; 32(1): 2589. https://doi.org/10.59400/adecp2589

ARTICLE INFO

Received: 14 January 2025 Accepted: 16 January 2025 Available online: 22 January 2025

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Copyright © 2025 by author(s). Advances in Differential Equations and Control Processes is published by Academic Publishing Pte. Ltd. This work is licensed under the Creative Commons Attribution (CC BY) license. https://creativecommons.org/licenses/ by/4.0/ **Abstract:** Mathematics serves as the fundamental basis for innovation, propelling technological advancement. In the forthcoming decade, the convergence of differential equations and control processes is poised to redefine the frontiers of scientific exploration. The integration of artificial intelligence and machine learning with differential equations is set to inaugurate a new era of problem-solving, enabling the extraction of latent physical insights and accelerating solution discovery. Multi-scale modeling, with its capacity to span disparate physical domains, has the potential to resolve long-standing puzzles in fields such as fluid mechanics and nanoscience. Furthermore, the integration of fractal geometry with differential equations holds the promise of novel perspectives for understanding and optimizing complex systems, ranging from urban landscapes to turbulent flows. The integration of artificial intelligence (AI) with control innovations is poised to play a pivotal role in the development of next-generation technologies, with the potential to transform diverse sectors such as medicine, communication, and autonomous systems. This paper explores these developments, highlighting their potential impacts and emphasizing the necessity for interdisciplinary collaboration to leverage their full potential.

Keywords: AI; machine learning; multi-scale modeling; turbulence; fractal geometry; nanotechnology; control processes

1. Introduction

Mathematics has exerted a profound and often unacknowledged influence on the development of modern technology. It provides the fundamental framework for understanding the natural world and engineering solutions. The employment of differential equations, which elegantly describe the dynamic relationships between variables and their rates of change, has been instrumental in modeling a vast array of phenomena. Control processes, in contrast, represent the strategic mechanisms employed for the purpose of manipulating these systems to achieve specific outcomes.

As we stand at the threshold of a new technological era, the synergy between differential equations and control processes is emerging as a hotbed of innovation. The ensuing decade is poised to witness a quantum leap in these fields, with far-reaching implications across multiple disciplines. These advancements hold the potential to enhance our understanding of the fundamental laws of nature while concomitantly driving a paradigm shift in our modes of living and working.

2. AI-powered problem solving: Unleashing the potential of data and physics

The integration of artificial intelligence and machine learning with differential equations is affecting a paradigm shift in the manner in which complex problems are approached. By leveraging the power of deep learning architectures and vast datasets, we can now decode the intricate physical principles encoded within differential equations.

Within the domain of fluid dynamics, for instance, neural networks are trained on substantial data derived from flow simulations and experimental measurements. This enables them to predict turbulent flow patterns with unprecedented accuracy. The concept of "physics-informed AI" has been shown to expedite the solution process and to uncover new facets of the underlying physical phenomena. For instance, in [1], the concept of point solution was introduced, which enables highly accurate estimation of the solution at a specific point. When multiple points are involved, this concept can be integrated with AI networks to address complex problems, such as weather forecasting [2] or tsunami prediction [3].

Furthermore, the integration of ancient mathematical algorithms [4–7] with modern AI techniques underscores the enduring relevance of mathematical principles. The capacity of AI to process multimodal data underscores its potential for applications in clinical care and other domains, as evidenced by [8]. The continuous evolution of this synergy is expected to open new frontiers in human-AI interaction and other crucial areas, as discussed in [9].

3. Multi-scale modeling: Bridging the micro and macro worlds

The exploration of multi-scale architectures and multi-physical field couplings is on the brink of a major breakthrough. In the domain of fluid mechanics, the Navier-Stokes Equations have historically posed significant challenges in fully encapsulating the intricacies of turbulence. However, multi-scale models offer a glimmer of hope in this regard. Turbulence frequently originates at the nanoscale, where the fluid exhibits unique discontinuities.

These multi-scale models possess the remarkable capacity to integrate the deterministic domain of Newtonian mechanics with the uncertainties inherent in quantum mechanics. This capacity renders them a formidable instrument in nanoscience, with the potential to elucidate some of the most perplexing enigmas in thermodynamics and physics. For instance, research in multiscale habitat selection modeling [10] and multiscale materials modeling [11] has already made significant strides.

Triboinformatics [12], an emerging interdisciplinary field, combines tribology and informatics to study frictional phenomena. By analyzing large amounts of data related to friction processes, this field aims to optimize tribological systems and enhance the efficiency and durability of mechanical assemblies across various industries.

4. Fractal frontiers: Connecting mathematics and the real world

The fractal geometry paradigm has introduced a revolutionary way of perceiving complexity. Specifically, the two-scale fractal geometry [13,14] provides a novel perspective by observing the world at diverse scales. This approach has the potential to render mathematical concepts more accessible and applicable to real-world problems.

In the domain of urban planning, fractal models facilitate the visualization of urban growth and evolution, thereby capturing the intricate patterns of infrastructure expansion and population distribution. The integration of differential equations with two-scale fractal derivatives facilitates the prediction of traffic flows, in addition to the management of the complex data analytics of individual vehicles and resource allocation within urban systems. This enhancement of urban design and promotion of sustainability is a key benefit.

In the study of turbulent fluids, the traditional mass conservation equations must be adapted in fractal space. By incorporating two-scale fractal dimensions into the temporal and spatial domains, as outlined by the fractional spatio-temporal relation [15], significant advancements may be achieved in the near future in the field of turbulence modeling.

5. AI-driven control innovations: Pioneering the future of technology

The forthcoming decade will be characterized by the emergence of AI-driven control as a catalyst for technological transformation. At the molecular level, the employment of nano-robots will necessitate the implementation of highly precise and adaptable control strategies. Algorithms of a reinforcement learning nature will be utilized to facilitate the training of these diminutive machines for such tasks as targeted drug delivery within the human body. This technological advancement has the potential to transform the medical field, enabling minimally invasive treatments and early disease detection.

The advent of 6G technology [16,17] will see intelligent control systems playing a pivotal role in the management of ultra-dense networks and ultra-low latency applications. The propagation of millimeter-wave signals in complex urban environments will be modeled using differential equations, while artificial intelligence (AI)-based controllers will optimize network resource allocation in real time. This integration of technology will ensure seamless connectivity for various applications, including augmented reality, virtual reality, and the Internet of Things.

Unmanned systems, including self-driving cars and drones, will achieve higher levels of autonomy. Fuzzy neural network control, enhanced by deep learning, will handle the uncertainties and nonlinearities in real-world driving conditions. The capacity of autonomous vehicles to formulate swift yet secure resolutions in intricate traffic scenarios will be thoroughly exhibited, while unmanned aerial vehicles will possess the capability to traverse challenging terrains for tasks such as search and rescue, infrastructure inspection, and precision agriculture.

6. Conclusion

The forthcoming decade is poised to witness significant advancements at the nexus of differential equations and control processes. These advancements promise to not only deepen our understanding of the natural world but also to reshape the way we live, work, and interact with technology. Mathematics is for innovation, invention, and revolution. It is the silent catalyst that propels humanity's progress, unlocking doors to unimagined possibilities and, more importantly, it is the shortcut to realizing one's life ideals.

It is incumbent upon the research community to wholeheartedly embrace these frontiers and foster interdisciplinary collaboration. Through the integration of expertise from diverse fields, we can fully realize the potential of these powerful mathematical tools and propel the next wave of technological innovation. Mathematics, as the driving force behind innovation, invention, and revolution, is pivotal to unlocking a future filled with endless possibilities.

Conflict of interest: The author declares no conflict of interest.

References

- 1. Liu YP, He JH. A fast and accurate estimation of amperometric current response in reaction kinetics. Journal of Electroanalytical Chemistry. 2025; 978: 118884.
- He JH. An Old Babylonian Algorithm and Its Modern Applications. Symmetry. 2024; 16(11): 1467. doi: 10.3390/sym16111467
- 3. Dee DP, Uppala SM, Simmons AJ, et al. The ERA-Interim reanalysis: Configuration and performance of the data assimilation system. Quarterly Journal of the Royal Meteorological Society. 2011; 137(656): 553–597.
- 4. Wang Y, Hou WF, Gepreel K, Li HJ. A fractal-fractional tsunami model considering near-shore fractal boundary. Fractals. 2024; 32(2): 2450040.
- Khan WA, Arif M, Mohammed M, et al. Numerical and Theoretical Investigation to Estimate Darcy Friction Factor in Water Network Problem Based on Modified Chun-Hui He's Algorithm and Applications. Mathematical Problems in Engineering. 2022; 8116282. doi: 10.1155/2022/8116282
- 6. He CH. An introduction to an ancient Chinese algorithm and its modification. International Journal of Numerical Methods for Heat & Fluid Flow. 2016; 26(8): 2486–2491.
- 7. Li XJ, Zhao R. Physics-informed deep ai simulation for fractal integro-differential equation. Fractals. 2024; 32(1): 2450022.
- Xiang JX, Wang XY, Zhang XM, et al. A vision-language foundation model for precision oncology. Nature. 2025; doi: 10.1038/s41586-024-08378-w
- 9. Thorp HH, Vinson V, Kmec L. Steady going in 2025. Science. 2025; 387(6729): 7.
- McGarigal K, Wan HY, Zeller KA, et al. Multi-scale habitat selection modeling: A review and outlook. landscape Ecology. 2016; 31(6): 1161–1175.
- 11. Schmauder S, Schäfer I. Multiscale materials modeling. Materials Today. 2016; 19(3): 130–131.
- 12. Nosonovsky M, Aglikov AS. Triboinformatics: Machine learning methods for frictional instabilities. Facta Universitatis Series Mechanical Engineering. 2024; 22(3): 423–433.
- Liu YP, He JH, Mahmud MH. Leveraging lotus seeds' distribution patterns for fractal super-rope optimization. Fractals. 2024. doi: 10.1142/S0218348X24501433
- 14. Zhang TR, Anjum N, Tian D, Alsolami AA. Fast and accurate population forecasting with two-scale fractal population dynamics and its application to population economics. Fractals. 2024; 32(5). doi:10.1142/S0218348X24500828
- 15. Wang KL, He CH. A remark on Wang's Fractal Variational Principle. Fractals. 2019; 27(8): 1950134.
- 16. Tian D, Huang ZX, Xiang JJ. A modeling and experimental analysis of fractal geometric potential mems in the context of the development of 6G and beyond. Fractals. 2024. doi: 10.1142/S0218348X2450124X

17. Zeng Y, Zhang R, Lim TJ. Wireless Communications with Unmanned Aerial Vehicles: Opportunities and Challenges. IEEE Communications Magazine. 2016; 54(5): 36–42.